

## A Study on Photonic Crystals and How They Use

Naikode Govind Ratan, PhD Scholar, Department of Physics, SunRise University  
Dr. Rajkumar Maurya, Professor, Department of Physics, SunRise University

### Abstract

By discussing the fundamental ideas and principles that underlie these artificial materials, as well as their capacity to control light and make possible unusual optical phenomena, this paper provides an introduction to photonic crystals. The negative refraction of light, the anomalous electromagnetic dispersion known as the superprism effect, and the possibility of superlensing also known as subwavelength focusing-are just a few examples that we will concentrate on. Because they are based on direct solutions to Maxwell's equations, these very general results may be applicable to numerous fields of science and technology.

**Keywords:** photonic crystals, negative refraction, superlens, superprism

### 1. INTRODUCTION TO PHOTONIC CRYSTALS

Materials known as photonic crystals exhibit periodic changes in their electromagnetic (EM) Properties on a timescale that is comparable to the wavelength of light, particularly when there is a lot of contrast. The photonic lattice's intricate structures and Maxwell's equations completely control the propagation of classical EM waves within these materials. The three-dimensional crystal structure can be extremely complex, influencing light propagation in a highly nontrivial way and sometimes exhibiting spectacular characteristics that are unfamiliar to conventional uniform material optics [1] [2].

The periodic scattering potentials in photonic crystals<sup>1, 2</sup> modify the quantum-mechanical motion of electrons in a manner that is comparable to that of crystalline solids, which is why their physics is frequently compared to that of photonic crystals. A position-dependent permittivity ( $\epsilon$ ) typically describes the modes of light propagation in a given photonic lattice, which is the fundamental problem. The stationary-state representation of the Maxwell equations can be represented by  $\nabla \times \mathbf{H} = \mu \epsilon \mathbf{E}$ . The solution to Eq. The fundamental ideas of the electron hand theory can be used to classify  $\mathbf{F}$  in a photonic crystal. With a Bloch wavevector  $\mathbf{k}$  in a Brillouin zone, the eigenmode  $\mathbf{F}$  can be made Bloch-periodic, according to the Bloch's theorem. After that, the eigenfrequency shows up as a function of  $\mathbf{k}$  and the band index  $n := n(\mathbf{k})$ , and shows how the Brillouin zone's variation in  $\mathbf{k}$  affects the photonic band structure. In a frequency range where eigenmodes are prohibited, there may be a photonic band gap. The numerical methods developed in studies of electron band structure, such as plane-wave expansion <sup>4</sup> and the Korringa-Kohn-Rostoker method, can be used to calculate actual photonic band structures. On the other hand, electron Bloch waves in crystals and EM eigenmodes in photonic crystals differ physically in a number of ways. The principle of photonic crystals' extreme generalizability is particularly significant. This is because Maxwell's equations do not have any fundamental lengthscales, and the photonic lattice can be scaled to any frequency with the band structure [3] [4].

Consequently, the same dimensionless parameters can be used to "scale" a system designed for the microwave regime to other wavelengths, such as the optical regime. This is very different from the electronic case, where the system's natural lengthscale is set by the Bohr radius. Additionally, the photonic band structure has more information about light polarization than its scalar-wave counterpart in electronic problems because EM waves are vector fields. Last but not least, it is important to note that photonic band structure numerical results are almost always accurate within the linear response approximation and can be more reliable than electronic band structure numerical results, which are almost always complicated by electron-electron interaction and Fermi statistics [5] [6].

In fact, light cannot travel in any direction because there is a photonic band gap at a variety of frequencies. This has not only resulted in novel photon-atom bound states that alter the fundamental physics of light emission, but it has also given rise to the idea of fundamental building blocks for optical materials that can be utilized to construct applications-relevant devices. For flexible light control, intentional defect structures within the band gap add a new design dimension. In order to produce ultra-low threshold lasers and resonance channel add-drop filters, ultrahigh-Q cavities can be introduced as point defects in a perfect crystal. Line

defects can guide light through extremely sharp corners, forming channels for effective light transportation. Furthermore, current planar lithographic methods can control and manipulate light in all three dimensions by combining the indexguiding mechanism of slab waveguides with two-dimensional photonic band gap effects. Photonic crystals may be used to modify the properties of light in a manner similar to that of band-gap engineering, which has been used in semiconductor electronics in the past. These developments echo those of the past.

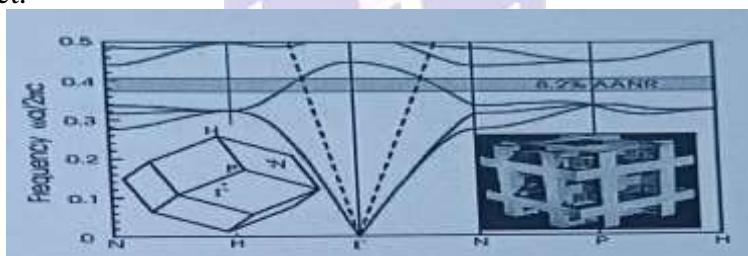
Using experimental and computational methods, these researchers investigated the effects of photonic-crystal dispersion relations on the direction of light flow, discovered the superprism phenomenon, and discovered an effective negative index of refraction for light. The superprism effect has also been studied in detail in two-dimensional (2D) triangular optical lattices<sup>25-28</sup> and in three-dimensional (3D) photonic crystals [7] [8] [9].

In this paper, we discuss how photonic crystals can be used to achieve negative refraction of light without using a negative index. Negative refractive index has recently been observed in microwave left-handed materials and was further proposed to lead to the formation of a perfect lens.

Next, two different superprism effects are identified and their distinct effects on radiation propagation are discussed. We also show that photonic crystals can focus light to subwavelength resolutions and extend our investigation to evanescent waves. Photonic crystals are an appealing material option for the development of novel technologies across a wide range of scientific and technological fields because they are a direct result of Maxwell's equations and should therefore have a wide range of validity [9] [10] [11].

## 2-THE SUPERPRISM EFFECT:

In this section, we'll talk about two kinds of effects with unusually high electromagnetic dispersion, which can be several orders of magnitude higher than dielectric materials' intrinsic dispersion. Kosaka introduced the first type, which primarily makes use of photonic crystal group-velocity dispersion properties. The other type is based primarily on the phase-velocity dispersion of a photonic crystal, and it is the result of pioneering work. As we'll see, these are two effects at opposite extremes of the photonic crystal dispersion surface that are physically distinct but connected. As a result, we will refer to either one using the term "superprism effect."



**Figure Ss (Color) Band structure (red) of a bec lattice of air cubes in dielectric whose parameters are given in the text**

The agile beam steering only occurs for light waves traveling within the crystal in the above superprism effect. Once light leaves the photonic lattice through an output facet, the large angular separation between beams entering a prism-shaped photonic crystal disappears. This is because the most important factor in determining the final beam direction is the Bloch-wavevector  $k$ , also known as the crystal's phase velocity of light: Conserving  $k$  along the exit surface is necessary. Despite the large change in the direction of  $k$ , the change in  $k$  within the crystal is actually very small because the group-velocity superprism effect occurs in a region of the dispersion surface with a large curvature. According to Figure, in order to spatially separate light beams using the group-velocity based superprism effect, a substantial crystal is required. Naturally, one would ponder the possibility of a superprism effect in  $k$ , in

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which the direction of light outside the crystal can be controlled with high sensitivity. Air may then take the place of the large space region used to separate light, and the crystal's size may shrink as a result. For frequencies that are close to the photonic band gaps, the experiments carried out by Lin indicate that a dispersion increase of approximately 20% is to be anticipated. However, this dispersion in  $k$  is about an order of magnitude smaller than what Eq predicts and is comparable to that of a conventional grating operating in the grazing-angle limit. 4. In fact, photonic crystals can be used to achieve a much greater magnitude of phase-velocity dispersion, as we demonstrate below [11] [12] [13] [14].

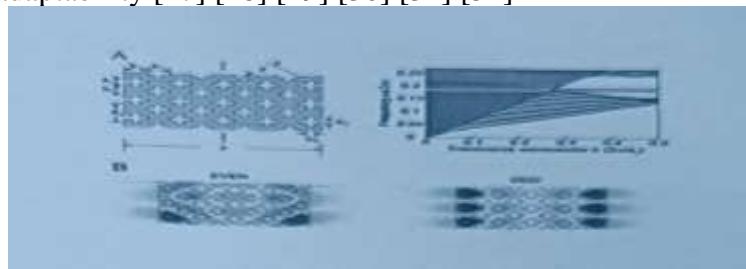
The use of adiabatic-tapering interfaces, similar to those found in the waveguide field is shown to be a systematic approach to increasing coupling efficiency into bulk crystals. The design criteria for the taper are simply that it should provide a continuously and slowly varying environment for light to move from one medium to the other, without creating a photonic band gap. We can simply use intermediate cells with the same lattice constant  $a$  but smaller dielectric rods to gradually reduce the size of the rods until they reach zero to taper the checkerboard crystal to free space. Fig. For the same photonic crystal, the calculated transmission and lateral shift results are depicted in Figure with additional taper layers on both sides to facilitate a smooth transition from the vacuum to the photonic crystal. Even at a mere taper thickness of four periods, the additional taper layers clearly reduce the Fabry-Perot oscillations and increase the transimssion to close to unity for a wide frequency range. For example, with an 8-period taper, lateral shifts of more than 1008, or an approximate refraction-angle magnitude greater than 80, can be achieved with an efficiency greater than 80 percent. This improvement gets better as the number of tapering layers increases. In the presence of the taper structure, the lateral shifts of the transition layers,

which are typically positive, will slightly alter the location where  $L$  crosses 0. For linear tapers, the envelope of the reflection coefficient is generally inversely proportional to the square of the taper length, as in the theory of waveguides. Therefore, the efficiency issue in photonic crystal extraordinary dispersion processes can be solved by achieving good coupling very close to the band edge with sufficiently long tapers [14] [15] [16] [17] [18]

### **3- SUBWAVELENGTH IMAGING**

We've seen in the previous sections that photonic crystals can be used to control the properties of waves as they travel, resulting in unusual phenomena. We look at how photonic crystals affect evanescent waves, which are characterized by  $k_{ip}/c$ , in this section. The extremely minute, subwavelength details that rapidly decay away from the source are represented by these waves. Even though traditional optical instruments like lenses and mirrors are able to focus waves that are moving in a particular direction, they are unable to change evanescent waves, which remain exponentially small after being transmitted. Using a slab of left-handed material with  $\epsilon$  and  $\mu$ , which is predicated to amplify evanescent waves, was one novel way to manipulate evanescent waves.<sup>24</sup> Both the propagating waves and the evanescent waves emitted by a point source placed in front of the slab can then be captured by the slab and refocused into a perfect point image behind the slab. In this section, we demonstrate that the negative-refractive photonic crystal slab discussed in Section 2 can be utilized to produce focused images with subwavelength details and to amplify a variety of evanescent waves. Using a coordinate system with  $x$  parallel to the slab and  $z$  perpendicular to the slab, we integrate the transmission complex field for planewaves of various transverse wavevectors to calculate the image of a TE point source behind the slab. The image region is represented by the region  $z > 0$ . The image shows a variety of distinct patterns that are strongly influenced by the coupling to the surface photon states for slightly different frequencies across the flat surface bands. Figure depicts the in-depth results that demonstrate the delicate

interaction between evanescent and propagating waves.[19] [20]. If the evanescent waves are amplified to a strength comparable to that of propagating waves, an isolated intensity maximum with a width of approximately 0.7 can be realized in the image space for  $0.193(2c/a)$ . In addition, some transmitted evanescent waves can have such an extraordinarily elevated amplitude that they dominate over all other evanescent and propagating modes due to the resonant nature of the current situation (no loss is assumed) and the extremely small group velocities of the bound photon modes. At  $0.192(2c/a)$ , this causes the enhanced surface resonance effect, which results in large field oscillations close to the crystal surface and causes the transverse image profile to become delocalized and ceases to produce a single peak. Additionally, at  $0.191(2c/a)$ , where the evanescent waves are amplified to such an extent that an intermediate imaging behavior emerges, a circumstance that is particularly intriguing [21] [22] [23] [24]. In this scenario, a distinct intensity peak with a size of 0.45 that is significantly below the wavelength may appear within the plane of AANR focusing, but there is no intensity maximum at  $z > 0$ . As a result, the pattern that was considered in the initial perfect lens proposal is very similar to this one [25] [26]. It is impossible to achieve these distinct imaging pattern regimes using conventional geometric optics because of the delicate balance between far and near fields. Photonic crystals are a powerful and beautiful option for focusing and manipulating light at subwavelength scales, particularly in the optical regime, thanks to their remarkable adaptability and adaptability [27] [28] [29] [30] [31] [32]



**Figure . (Color) Bound photon modes with TE (magnetic field perpendicular to the plane) polarization in a 2D photonic crystal slab.**

## CONCLUSIONS

Photonic crystals have made possible a variety of novel optical phenomena that we have discussed in this paper. Photonic crystals provide a real-world illustration of negative refraction, which can occur in materials with no effective negative index. In some cases, their intricate Bragg scattering effect resembles abnormal electromagnetic dispersion, which can be used to alter light's group velocity or phase velocity. These processes can occur with high efficiency in crystals that have been designed correctly. Photonic crystals can also be used to focus light to subwavelength resolutions and amplify evanescent waves.

Even though our discussion focuses mostly on dielectric crystals, crystals with metallic components can be easily observed in the microwave regime thanks to an analysis that is very similar to ours. We are confident that these unusual effects are only a small portion of the extensive and unconventional electrodynamics made possible by photonic crystals due to their extreme versatility. We hope that the reader of this paper will find it helpful to learn the fundamentals of photonic crystals and come up with new ways to use these new materials on their own.

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